$3D_landslide_detection_using_CloudCompare$

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Beyond 2D landslide inventories and their rollover: synoptic 3D inventories and volume from repeat lidar data



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1 Presentation of the data

Location : The Towy-Robson catchment area



Table 1. Information on the lidar data used in this study.

	Pre-earthquake lidar	Post-earthquake lidar
Date of acquisition	13 Mar 2014–20 Mar 2014	3 Dec 2016–6 Jan 2017
Commissioned by/provided by	USC-UCLA-GNS science/NCALM	Land Information New Zealand/AAM NZ
Availability	https://doi.org/10.5069/G9G44N75	Upon request from https://canterburymaps.govt.nz/about/feedback/
Original point density (points m^{-2})	9.02	19.2 ± 11.7
Number of ground points	10 660 089	63 729 096
Ground point density (points m ⁻²)	3.8 ± 2.1	11.5 ± 6.8
Vertical accuracy (m, as ± 1 SD)	0.068-0.165	0.04
Study area (m ²)	5 253 133	5 253 133

2 Before starting

2.1 Some good practice with CloudCompare:

- 1. Rename new point clouds with an explicit name
- 2. Clone point clouds before executing an irreversible operation
- 3. Save regularly

2.2 Set the global shift file

When loading (or generating) an entity with very big coordinates (typically greater than 105), CloudCompare will warn the user about this and suggest to shift (or rescale) the entity in order to work in a local coordinate system with smaller coordinates:



It is strongly advised to shift and scale the entities in this case. In "command line" mode, you have to modify the "global_shift_list.txt" file with your own shift generally located in 'C:/Program Files/CloudCompare'.

The format is the following. All values are separated by a semicolon character (;): name; shift(X); shift(Y); shift(Z); scale;

3 Getting started

You can use your own data or download data from New Zealand here : https://filesender.renater.fr/?s=download&token=b6cddecf-a810-4f01-a395-21ef1ba4e857

You can also download the orthophotos of the study area here (1.2 Go): https://filesender.renater.fr/?s=download&token=70bc7a18-aaa9-4a0c-8fb9-6a93b4930bf1

The folder contains:

- Pre_EQ_LiDAR_2014.laz : LiDAR survey in 2014 along the hope fault collected by the National Center for Airborne Laser Mapping (available in Opentopography: https://doi.org/10.5069/G9G44N75)
- Post_EQ_LiDAR_2016.laz : *LiDAR survey in 2017*
- Study_area_polyline : polyline of the study area used to define the area of interest
- river : point cloud of the core points located in the river network.
- core_points.laz : the point cloud with the core points (but we will do our own core points)
- GIS/:
 - . orthophotos/
 - . Kaikoura_EQ_Towy_river.qgz: QGIS project with the orthophotos

For what follows, I assume your data are already co-registrated.

4 Workflow



4.1 Creation of core points

While M3C2 can be applied on all points, the algorithm can use an accessory point cloud, called *core points*. In our case, core points constitute a regular grid with constant horizontal spacing generated by the rasterization of one of the two clouds.

Usually the core point should be created from the pre-EQ dataset to estimate normals. However, here we are going to create the core points from the pre-EQ dataset because the point density is much higher in the post-EQ point cloud and the classification is better.

Select the post-EQ point cloud and click on the Rasterize tool and create a regular grid of 1 m spacing.

Rasterize		— 0	
Grid		core points (7 055 048 points)	
step	1.000000 🚔 Edit grid		
size	4296 x 3057		
active layer	Height grid values 🗸 🗸		
range	10886.6 [-9999 ; 887.64]		
Projection			
direction	z v		
cell height	minimum 🗸		
interpolate SF(s)	minimum value		
resample input cloud			
Empty cells			
Fill with internola	te V		
First collector			
Empty cell value -9999,000			
Max edge length 40.00000			
e	Jodate grid		
Export Contour plot	Hillshade Volume		
Cloud	Mesh		
Export per-cell statistics as SP	F(s):		
population	nin height		
average height n	nax height		
height std. dev.	neight range		
		1000	
Raster	Image Matrix		

4.2 Geomorphic change detection

4.2.1 3D-M3C2 with the registration error

A bit of nicknames: M3C2 has the option of computing the distance vertically, which by passes the normal calculation, and we use this option several times in the workflow. We use the abbreviation "vertical-M3C2" in these cases and "3D-M3C2" otherwise.



in paramete Scales	ers Norma	ls Advanced	Precision maps	Output		
Normals	diameter = 10	0.000000		•	Compute normals (on core points)	~
Projection	diameter = 5	000000		-	max depth = 30.000000	
O use off	er doud	ann aniste (TD 2)	ar]			
		core points [10 3.	25]			· ·
🛃 Registra	ation error 0	.200000				Guess params

Estimation of the registration error -> quality control on flight lines or standard deviation on stable areas

4.2.2 3D-M3C2 on NaN d = 10m

For core points in low-point-density areas, where a confidence interval could not be estimated due to insufficient points, a second application of 3D-M3C2 is performed at a larger projection scale d = 10 m. These core points generally correspond to ground points under canopy on steep slopes.

- 1. Display the SF "distance uncertainty" and click on the filtering tool icon $\overleftarrow{}$.
- 2. Click on "Split"

It results in two point clouds : one with values and one with NaN.

- 3. Segment the NaN point cloud with the provided .shp file or with the segmentation tool ^{*} to delineate your area of interest.
- 4. Apply 3D-M3C2 with d = 10 m. The core points here is the NaN point cloud.

At this stage we have two point clouds: one with 3D-M3C2 results using a projection scale d = 5 m and a second one with 3D-M3C2 results using d = 10 m.

4.2.3 (Optional) Applying multiple cylindre M3C2 : the approach

In M3C2, *pmax* must be chosen to be larger than the largest topographic change to be measured. Thus, *pmax* can be as large as several tens of meters in landslide inventories. This poses a potential issue in highly curved features of the landscape such as narrow ridges or gorges with steep flanks where the cylinder can intercept the same point cloud twice (double-intercept issue), resulting in an incorrect distance calculation. Thus, we have modified the M3C2 algorithm to avoid the doubleintercept issue. A new iterative procedure progressively increases the depth of the cylinder up to *pmax*, by intervals of 1m for each core point, and checks for the stability of the measured distance: if the distance is stable for two successive iterations, it is considered as the final M3C2 distance for this core point.

The best approach is (a new version of M3C2 is in progress to do it automatically and will be available in Cloudcompare):

- While p(i) < pmax, $p(i+1) = 2^*p(i)$. Si d5 p(i+1) = d5 p(i) -> add them to the final core points . Otherwise, we continue

However, it will be a bit long to do it in Cloucompare, so today we will apply a simpler approach which consists on the following step:

Steps in Cloudcompare:

1. Rename all SF with suffix p30

2. 3D-M3C2 on d=5m with pmin=1.4m (keep normal with 'use core point normals' and quote use original cloud)

3. Rename all newest SF with '_p1.4' at the end of the name

4. 3D-M3C2 on d=5m with pmin = 2.8m (keep normal with 'use core point normals')

5. Select the SF "distance_uncertainty" calculated with p=2.8 m and split the point cloud using the filtering

6. From the point cloud with NaN value, remove all SF except results from 3D-M3C2 with p=30m and rename the point cloud to '3D-M3C2_p=30'

Scalar the other cloud: Edit Field Arithmetic 7. On > >-> $M3C2_distance(p=2.8m)/M3C_distance(p=1.4m)$

8. Extract all points with M3C2 distance(p=2.8m)/M3C distance(p=1.4m) $\neq 1$

9. For the point cloud with M3C2_distance(p=2.8m)/M3C_distance(p=1.4m) = 1 \rightarrow M3C2 à 1.4m

10. All the other points \rightarrow 3D-M3C2 pmin = 30 m

11. Rename all SF

12. Merge all point clouds

Repeat these steps for 3D-M3C2 with d = 10 m.

(Optional) Re-calculate significant changes (available in the python version) 4.2.4

M3C2 provides the uncertainty in the computed distance at the 95% confidence level based on local roughness, point density and registration error as follows:

$$LoD_{95\%}(d) = \pm t(DF)(\sqrt{\frac{\sigma_1(d)^2}{n_1} + \frac{\sigma_2(d)^2}{n_2}} + reg)$$

with

$$DF = \frac{\left(\frac{\sigma_1(d)^2}{n_1} + \frac{\sigma_2(d)^2}{n_2}\right)^2}{\left(\frac{\sigma_1(d)^4}{n_1^2} + \frac{\sigma_2(d)^4}{n_2^2}\right)}$$

1

where $LoD_{95\%}$ is the level of detection; t is the two-tailed t statistics with a confidence level of 95% and a degree of freedom DF (Borradaile, 2003); $\sigma_1(d)$ and $\sigma_2(d)$ are the standard deviation of distances of each cloud, at scale d;measured along the normal direction; n_1 and n_2 are the number of points in each cloud at that scale; and *reg* is the co-registration error between the two epochs.

The original M3C2 algorithm uses a value of t equal to 1.96, the asymptotic value of the two-tailed t statistics when F is infinite, and the $LoD_{95\%}$ is only computed if $n_1 > 4$ and $n_2 > 4$. As will be shown later, the low point density of the pre-EQ data in forested areas resulted in values of n_1 varying between 5 and 15, in which case t (F(n1;n2)) is significantly larger than 1.96. For instance, when $n_1 = n_2 = 5$, F = 4 and t = 2.776. To avoid underpredicting $LoD_{95\%}$ in low-point-density areas, we choose to apply the strict two-tailed t statistics rather than the simplification used in the CloudCompare implementation of M3C2.

4.2.5 Extract significant changes

To extract significant changes, simply select the scalar field 'Significant change', then click on the filtering tool $\xrightarrow{\text{filtering}}$ and export all points with a value > 0.

4.2.6 Extract topographic changes located in the river network

Changes located in the river bed, and likely specifically related to river dynamics and not to landslide deposits, are manually removed using the post-EQ orthoimage. Along with the selection of the stable areas, this is the only manual phase of the workflow.

2 possibilities:

1. Using the provided file "river.laz": you can simply compute a cloud-to-cloud distance 1 for which the compared cloud is the 'Significant changes' and the reference cloud is the 'river' point cloud. Then remove all points with a Cloud-to-cloud distance value < 5 m

2. If you are working with your own dataset: Select the segmentation tool 2° , delineate the river network and then extract the points located outside of the polygon you created.

4.3 Segmentation into individual cluster

4.3.1 Extract significant negative and positive changes

Select the significant changes point cloud and active the 'M3C2 distance' scalar field. Then select the filtering tool , change the max value to zero and then click on 'split'.

4.3.2 Vertical-M3C2

- 1. Rename all the scalar fields resulting from the 3D-M3C2 calculation (for example you can add '_3D' at the end)
- 2. Select the Pre-EQ and Post-EQ point clouds and click on the M3C2 plugin icon The core points are the point clouds with erosion areas and deposits areas. Do not forget to select the *'vertical mode'* to compute normals.
- 3. Rename the newly created 'M3C2 distance' SF 'M3C2_distance_vertical'.

🞇 M3C2 distance									?	\times
Cloud #1 Pre_EQ_LiDAF	R_2014 - Cloud [ID 264]									
Cloud #2 Post_EQ_LiDA	R_2016 [ID 266]									6
Main parameters Norma	als Advanced Pre	acision maps Output	t							
Scales										
Normals diameter = 1	0.000000		•	Compute no	ormals	(on core points)			\sim	
Projection diameter = 5	.000000			max depth =	30.00	00000			-	
Core points										
 use cloud #1 subsample cloud #1 	1.000000									
 use other cloud 	Erosion [ID 294]								• •	
Registration error (0.200000							Guess	params	
							OK		Cance	
							OK		Cance	
M3C2 distance									?	×
Cloud #2	R_2014 - Cloud [10 264]								-	G
Main assumptions Normal	4R_2016 [ID 266]	o de la contra								
Calculation mode	als Advanced Pr	ecision maps Outpu	It							
O Default	🔘 Multi-sc	ale	0	Vertical		⊖н₀	rizontal			
Min = 25.421497	A V	Step = 25.421497			*	Max = 101.685988			*	
Use core points for n	ormal calculation									
Orientation										
Preferred orientation	+Z								~	
 Use origin point(s) 	Pre_EQ_LiDAR_2014 -	Cloud [ID 264]							~	

4.3.3 Segmentation by connected component

1. Select the point coud with negative M3C2 distance values and click on the Label connected components icon **EE**.

Connected Components		
Octree Level	11 (grid step = 1.96583)	
Min. points per component	20	
🛃 random colors (warning	: overwrites existing ones)	
	OK Cancel	

 A_{min} was set to 20 m² to be consistent with the area of the projection cylinder used to average the point cloud position in the M3C2 distance calculation, $\pi * (d/2)^2 = 19.6$ m² with d = 5 m.

2. Repeat the previous step for positive M3C2 distance values.

Let's see the effect of the octree level (or minimum distance between two clusters) on the results! You can try with an octree level of 10 $(D_m \sim 4 \text{ m})$ and of 9 $(D_m \sim 8 \text{ m})$.

4.4 Volume estimation (using python/Matlab or excel)

- 1. Select all the segmented landslides
- 2. Tools > Batch export > Export cloud info or E

All information about the different landslides will be stored in a .csv file that can then be analyzed using python/Matlab or excel.

4.5 Export result to a GIS format

1. Select all the landslide source or deposit point clouds, clone and Merge . While merging click on 'Yes' to generate a scalar field with the original cloud index.

Then we want to create a raster or a regular grid as we did to create core points. However, we want the points of the grid to be exactly in the same position than the core points.

2. Select the post-EQ_LiDAR point cloud (or the point cloud from which you created the core

points) and select \blacksquare . Then click on '*Edit grid*' and press '*OK*', update the grid and click on '*OK*'.

- 3. Select the point clouds where alle the landslide sources (or deposits) are merged and select
- 4. Go to 'Edit grid' and click on 'Last'. For empty cells 'leave empty' and update grid.

5. Click on raster and you can export your result in a .tif file format.

Now you can open this file in your favorite GIS software.

It is also possible to export the scalar fields!

4.6 Treatment of false detection (using python/Matlab or excel)

Owing to the simplified formulation of the $LoD_{95\%}$, it is possible for spatially correlated errors to create patches of statistically significant change that would appear after segmentation as false landslide detection.



Illustration of two types of labeled false detections. (a) A false detection located in a forest due to vegetation incorrectly classified as ground in the pre-EQ point cloud. The apparent negative topographic change creates a source. (b) A false detection due to pre-EQ intra-survey registration errors. Yellow points on the post-EQ orthoimagery (Aerial Surveys, 2017) and the M3C2 distance field indicate patches of significant change that are a false detection. They occur due to a complex combination of intra-line errors related to time-dependent attitude and position errors and intra-survey flight-line registration error.

As false detections mainly emerge from the errors in the data in relation to the amplitude of a real topographic change that we aim to capture, we first choose to analyze three metrics based on the 3D-M3C2 calculation:

- (1) the maximum 3D distance,
- (2) the mean $LoD_{95\%}$ and
- (3) the mean signal-to-noise ratio (SNR).

As the $LoD_{95\%}$ is a direct measure of the quality of the data (point density and roughness), classification errors of vegetation should be characterized by a significantly higher mean $LoD_{95\%}$ than actual landslide sources. The SNR is defined as the ratio between the 3D-M3C2 distance and the associated $LoD_{95\%}$ for each core point. This measure can be used as a confidence metric for each source.

$$SNR = \frac{3D \text{ M3C2 distance}}{LoD_{95\%}}$$

This ratio is defined for each core point and the mean is used at the scale of each landslide to filter artefacts.

In practice:

1. Select the point coud with negative M3C2 distance values and go to Edit > Scalar fields > Arithmetic

2. Compute the SNR ratio

Scalar field	ls arithmetics			
SF 1	M3C2 distance_3D	~		
operation	divided by	~		
SF 2	distance uncertainty_3D	\sim		
	1.000000	* *		
Update SF1 directly OK Cancel				

3. Rename the newly created scalar field 'SNR_ratio'

We also choose to take advantage of the ability of the 3D differencing approach to detect deposit areas to analyze the closest deposit distance (CDD). The CDD is defined for each provisional source as the closest downslope distance to a provisional deposit along the flow path using a D8 (deterministic eight-node) algorithm (Fairfield and Leymarie, 1991). This distance is calculated from the post-EQ DEM with the MATLAB-based TopoToolbox software (Schwanghart and Scherler, 2014).

5 A bit of Python

These are all the libraries you will need.

These are libraries you probably already have.

- numpy
- matplotlib
- os
- subprocess

These are those you probably have to install :

• pandas : a fast, powerful, flexible and easy to use open source data analysis and manipulation too

Installation with pip: 'pip install pandas' in your command prompt

- laspy : Python library for lidar LAS/LAZ Installation with pip: '*pip install laspy*' in your command prompt
- scikit-learn : Simple and efficient tools for predictive data analysis Installation : *'pip install -U scikit-learn'* in your command prompt

5.1 Filtering of false detection using the SNR ratio

As a reminder, the SNR is defined as the ratio between the 3D-M3C2 distance and the associated $LoD_{95\%}$ for each core point. This measure can be used as a confidence metric for each source.

```
[5]: # Definition of the functions
     def do_compression(filename):
         ......
         This function allows to compress a ".las" file to a ".laz" file.
         filename : path + filename
         .....
         query="laszip -i "+filename+" -olaz"
         subprocess.run(query)
         os.remove(filename)
     def write_new_SF(path,filename,SF_name,SF_array):
         .....
         This function allows to write a new scalar field from a LAS file
         SF_name: Name of the new scalar field
         SF_array : Values of this new scalar field
         .....
         import copy
         import os
         # rename the input file
         os.rename(path+filename+'.laz', path+filename+'_origin'+'.laz')
         # Set up our input and output files.
         inFile = laspy.file.File(path+filename+'_origin.laz', mode = "r")
         outFile = laspy.file.File(path+filename+'.las', mode = "w",
                 header = inFile.header)
         # Define our new dimension. Note, this must be done before giving
         # the output file point records.
         outFile.define new dimension(name = SF name,
                             data_type = 9, description = "Test Dimension")
         # Lets go ahead and copy all the existing data from inFile:
         for dimension in inFile.point_format:
             dat = inFile.reader.get_dimension(dimension.name)
             outFile writer set_dimension(dimension.name, dat)
         # Now lets put data in our new dimension
         # (though we could have done this first)
         # Note that the data type 5 refers to a long integer
         outFile.points['point'][SF_name] = SF_array
         inFile.close()
         outFile.close()
         do_compression(path+filename+'.las')
```

```
os.remove(path+filename+'_origin'+'.laz')
```

```
[6]: # Import libraries
import laspy
from laspy.file import File
import numpy as np
import subprocess
import os
```

```
[3]: # Read the .laz file and the scalar field 'id' corresponding to the id of each
      \rightarrow landslide sources
     path = 'D:/Post_doc/Summer_school_ptcloud_2022/3D_landslide_detection_python/
     \rightarrowLandslide_detection/res/'
     filename = 'landslide_sources'
     inFile = File(path+filename+'.laz', mode='r')
     id_landslide = inFile.points['point']['id']
     id_landslide_unique = np.unique(id_landslide) # create an array with all the
     \rightarrow landslide id
     SNR_ratio = inFile.points['point']['SNR_ratio']
     inFile.close()
     SNR_threshold = 1.45 # the value of the mean SNR ratio below which the
     \rightarrow landslide sources are considered as false detection.
     id SNR = np.copy(SNR ratio)
     for i in id_landslide_unique:
         SNR_ratio_ls = SNR_ratio[id_landslide == i] # select the SNR values for the
      \hookrightarrow landslide source with the id i
         mean_SNR = np.mean(SNR_ratio_ls) # Compute the mean
         if mean_SNR < 1.45 :
             id_SNR[id_landslide==i] = -9999 # we define -9999 as a new id for the
      → false detection to be easily removed later in CloudCompare
         else:
             id_SNR[id_landslide==i] = i # we keep the same id otherwise
     write_new_SF(path,filename,'id_landslide',id_SNR) # write a new scalar_field
```

Now you can open the newly created .laz file with Cloudcompare and see which landslide sources have been filtered out!

You can split the point cloud in function of the 'id' scalar field : Edit > Scalar fields > Split cloud (integer values)

5.2 Landslide analysis

5.2.1 Read the .csv file with pandas

```
[7]: # Import libraries
import pandas as pd
```

5.2.2 Display some landslide general information

```
[9]: def read_landslide_prop(path, filenames):
        .....
        This function allows to read and display some basic landslide properties.
        path: path to the landslide results
        filenames: dictionary with the sources and deposits filenames.
        .....
        # Read .csv files into a dataframe
        dataframes={'Sources': pd.read_csv(path+filenames['Sources'],sep=';
     # Create empty list to add values after
        number_of_clouds = []
        area range = []
        Total_area = []
        volume_range = []
        Total volume = []
        uncertainty_volume_range = []
        Uncertainty_Total_volume = []
        # Select Area, volume and uncertainty
        ## define the name of the scalar fields corresponding to the vertical-M3C2_{1}
     \hookrightarrow calculation
        ## and the 3D distance uncertainty
        vertical_M3C2 = 'Sum_M3C2_distance_vertical'
        dist_unc = 'Sum_3D_distance_uncertainty'
        for i in range(0,len(dataframes)):
            number_of_clouds.append(len(list(dataframes.values())[i]))
            area_range.append([list(dataframes.values())[i]['Points'].

_min(),list(dataframes.values())[i]['Points'].max()])
            Total_area.append(list(dataframes.values())[i]['Points'].sum())
```

```
volume_range.append([np.around(list(dataframes.

=values())[i][vertical_M3C2].abs().min(),2),np.around(list(dataframes.

=values())[i][vertical_M3C2].abs().max(),2)])

Total_volume.append(np.around(list(dataframes.values())[i][dist_unc].

=abs().sum(),0))

uncertainty_volume_range.append([list(dataframes.values())[i][dist_unc].

=min(),list(dataframes.values())[i][dist_unc].max()])

Uncertainty_Total_volume.append(np.around(list(dataframes.

=values())[i][dist_unc].sum(),0))

# Range data into a dataframe

df_dico={'Number of sources/deposits':number_of_clouds,'Area range (m<sup>2</sup>;_u

=>[min,max])':area_range,'Total area (m<sup>2</sup>)':Total_area,

'Volume range (m$^3$)':volume_range,'Total volume (m$^3$)':_u

=>Total_volume, '3D uncertainty on total volume':Uncertainty_Total_volume}

Dataframe = pd.DataFrame(df_dico,index=['Sources','Deposits'])
```

return Dataframe

[10]:		Number of sources/deposits Area range (m 2 ; [min,max]) \setminus
	Sources	1163 [20.0, 40444.0]
	Deposits	741 [20.0, 27894.0]
		Total area (m ²) Volume range (m\$^3\$) Total volume (m\$^3\$) \
	Sources	320589.0 [1.01, 169710.32] 182065.0
	Deposits	315780.0 [0.03, 151612.67] 174306.0
		3D uncertainty on total volume
	Sources	182065.0

174306.0

5.2.3 Landslide source distribution

Deposits

```
max_data = np.max(dataset)
    min_data = np.min(dataset)
    bins = np.logspace(np.log10(min_data),np.log10(max_data),num=N_bin) #__
 \rightarrow create bin in a logspace
    #distribution
    bin min = bins[:-1]
    bin_max = bins[1:]
    N = np.zeros(len(bin_min))
    N2 = np.zeros(len(bin_min))
    X = np.zeros(len(bin_min))
    for i in range(len(bin_min)):
         index = [(dataset>=bin_min[i]) & (dataset<bin_max[i])]</pre>
        if i == len(bin_min):
             index = [(dataset>=bin_min[i]) & (dataset<=bin_max[i])]</pre>
        N[i] = dataset[index].shape[0]
        X[i] = (bin_min[i] + bin_max[i])/2 # take the center of the bin
    if density == True:
        N = N/(bin max-bin min)
        N = N/dataset.shape[0]
        return X, N
    else:
        return X, N
def linear_fit(X,Y):
    111
    Function that compute a log-transformed linear fit model
    111
    x_test = X == 0
    x_test = np.max(x_test)
    y_test = Y == 0
    y_test = np.max(y_test)
    if x_test == True:
        \mathbf{Y} = \mathbf{Y} [\mathbf{X} = 0]
        X = X [X = 0]
    if y_test == True:
        X = X[Y = 0]
        \mathbf{Y} = \mathbf{Y} [\mathbf{Y} | = 0]
    p, v = np.polyfit(np.log10(X),np.log10(Y),deg=1,cov=True)
    std = np.sqrt(np.diag(v))
    print(p, std)
    ypred = 10**(p[1])*X**p[0]
```

```
from sklearn.metrics import r2_score
          print('R<sup>2</sup> = ', r2_score(np.log10(Y),np.log10(ypred)))
          return p, v, std, ypred, X,Y
[36]: import matplotlib.pyplot as plt
[41]: # Compute distribution
      dataset = df_source['Points'].to_numpy() # here we consider that the number of d_{LL}
      \rightarrow point is approximately the area, you can choose the landslide volume as well
      X, N = distribution log bin(dataset, N bin = 20, density = True)
      # Compute linear fit
      p,v,std, y_fit, X_fit,_ = linear_fit(X,N)
      # Plot results
      ymin, ymax = 1e-8, 1e-1
      xmin, xmax = 1, 2e5
      plt.figure(figsize=(11,9))
      # plot the data
      plt.plot(X,N,'o', markersize = 16, mfc='silver', mec = 'k',mew=2, label = '3D_L
      →inventory',zorder=4)
      plt.plot(X_fit,y_fit,'k-',zorder=4,linewidth=2)
      # plot parameters
      plt.tick_params(axis='both',which='major',length=8,width=2)
      plt.tick_params(axis='both',which='minor',length=4,width=2)
      plt.ylim(ymin,ymax)
      plt.xlim(xmin,xmax)
      plt.xscale('log')
      plt.yscale('log')
      plt.xticks(fontsize=26)
      plt.yticks(fontsize=26)
      plt.xlabel('Area (m<sup>2</sup>)', fontsize=28, fontweight='bold')
      plt.ylabel('p(A) (m-2)', fontsize=28, fontweight='bold')
```

 $[-1.83883188 \ 1.00709287]$ $[0.04318124 \ 0.13014635]$ $R^2 = 0.9912539680932435$

C:\Users\tbernard\Anaconda3-64bit\envs\papier_landslide\lib\sitepackages\ipykernel_launcher.py:24: FutureWarning: Using a non-tuple sequence for multidimensional indexing is deprecated; use `arr[tuple(seq)]` instead of `arr[seq]`. In the future this will be interpreted as an array index, `arr[np.array(seq)]`, which will result either in an error or a different result.

[41]: Text(0, 0.5, 'p(A) (m-²)')



6 References

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